SINGLE-PHASE SHUNT AND SERIES ACTIVE HARMONIC FILTERING FOR IMPROVING POWER QUALITY

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I SHUNT ACTIVE FILTERING

1. Introduction

The increasing use of power electronics-based loads (adjustable speed drives, switch mode power supplies, etc.) to improve system efficiency and controllability is increasing the concern for harmonic distortion levels in end use facilities and on the overall power system. The application of passive tuned filters creates new system resonances which are dependent on specific system conditions. In addition, passive filters often need to be significantly oversized to account for possible harmonic absorption from the power system. Passive filter ratings must be co-ordinated with reactive power requirements of the loads and it is often difficult to design the filters to avoid leading power factor operation for some load conditions. Active filters have the advantage of being able to compensate for harmonics without fundamental frequency reactive power concerns. This means that the rating of the active power can be less than a comparable passive filter for the same non-linear load and the active filter will not introduce system resonances that can move a harmonic problem from one frequency to another.

The shunt active filter concept uses power electronics to produce harmonic current components that cancel the harmonic current components from the non-linear loads. The active filter uses power electronic switching to generate harmonic currents that cancel the harmonic currents from a non-linear load. The active filter configuration investigated in this lecture is based on a pulse-width modulated (PWM) voltage source inverter that interfaces to the system through a system interface filter as shown in Figure 1. In this configuration, the filter is connected in parallel with the load being compensated. Therefore, the configuration is often referred to as an active parallel or shunt filter. Figure 1 illustrates the concept of the harmonic current cancellation so that the current being supplied from the source is sinusoidal. The voltage source inverter used in the active filter makes the harmonic control possible. This inverter uses dc capacitors as the supply and can switch at a high frequency to generate a signal that will cancel the harmonics from the non-linear load.

The active filter does not need to provide any real power to cancel harmonic currents from the load. The harmonic currents to be cancelled show up as reactive power. Reduction in the harmonic voltage distortion occurs because the harmonic currents flowing through the source impedance are reduced. Therefore, the dc capacitors and the filter components must be rated based on the reactive power associated with the harmonics to be cancelled and on the actual current waveform (rms and peak current magnitude) that must be generated to achieve the cancellation.

The current waveform for cancelling harmonics is achieved with the voltage source inverter in the current controlled mode and an interfacing filter. The filter provides smoothing and isolation for high frequency components. The desired current waveform is obtained by accurately controlling the switching of the insulated gate bipolar transistors (IGBTs) in the inverter. Control of the current waveshape is limited by the switching frequency of the inverter and by the available driving voltage across the interfacing inductance.

The driving voltage across the interfacing inductance determines the maximum di/dt that can be achieved by the filter. This is important because relatively high values of di/dt may be needed to cancel higher order harmonic components. Therefore, there is a trade-off involved in sizing the interface inductor. A larger inductor is better for isolation from the power system and protection from transient disturbances. However, the larger inductor limits the ability of the active filter to cancel higher order harmonics.

The Inverter (three-phase unit or single-phase unit as the case may be) in the Shunt Active Power Filter is a bilateral converter and it is controlled in the Current Regulated mode i.e. the switching of the Inverter is done in such a way that it delivers a current which is equal to the set value of current in the current control loop. This mode of operation of a PWM-VSI has been covered in detail in an earlier lecture. Thus the...
basic principle of Shunt Active Power Filter is that it generates a current equal and opposite in polarity to the harmonic current drawn by the load and injects it to the point of coupling thereby forcing the source current to be pure sinusoidal. This type of Shunt Active Power Filter is called the Current Injection Type APF.

2. A Single Phase Current Injection Type Active Power Filter

Single-Phase topology is assumed for purposes of explanation for the sake of simplicity. Whatever is covered here will be equally applicable for three-phase systems also with minor modifications. A simplified diagram of a single-phase APF is given in Fig.2 below.

![Fig. 2 A Single Phase Active Power Filter](image)

The control system maintains the average voltage across the capacitor constant against variations in line and filtering load on the APF. The Inverter is gated in such a way that the current I_L follows a reference current waveform set by the concerned control system. The voltage required at the terminals of Inverter output will be automatically made suitable for maintaining the required current in the L_L line, i.e. the Inverter is controlled in the 'current regulated' mode. The current delivered by the source I_s = I_o - I_L and it is desired that this current be a pure sinusoidal wave even when the load draws a highly distorted current wave. This is accomplished by making I_L equal to the harmonic current required by the load. Thus, there has to be a harmonic current calculator which will calculate the harmonic current to be generated by the Inverter in order to maintain the source current harmonic free. Under a loss free situation, the Inverter does not need to draw any active power. However, there will be losses in the resistances of inductor, switches etc. and switching losses when the Inverter is generating current. Unless these losses are compensated, the capacitor voltage will come down steadily. Hence the control of capacitor voltage involves drawing an in phase sinusoidal component of current from the source along with the required harmonic currents, i.e. the reference current for I_L should contain an appropriate amount of 180° component to maintain the D.C voltage across the capacitor.

It is indeed possible to make the Inverter deliver the reactive current demanded by the load along with its harmonic current requirement by providing suitable reference. In that case APF becomes an SVC - cum-APF or an APF-cum-SVC. In fact, it should by now be clear that, whether it does reactive compensation or not, the operation and control of this APF is almost the same as that of the SVC with Current Regulated Control. The basic principles involved are the same. But, usually in an SVC harmonic filtering is not attempted along with Fundamental frequency VAr compensation since the range of switching frequencies needed for APF action is much higher than the frequency needed for SVC action. The kVAR rating of SVC for a load will be much higher than the kVA rating needed for an APF. Hence it is better to use a small kVA rated Inverter with high switching frequency (thereby demanding IGBTs/MOSFETs) for the APF function and a high power Inverter with low switching frequency for (thereby permitting the use of thyristors and GTOs) for SVC action. In fact, if the two jobs are separated this way, it is possible to run the SVC at a still lower frequency with the APF helping to cancel the harmonics generated by the low frequency switching of SVC partially. Such systems have been made at sub-transmission level. Notwithstanding the above, the continuous improvement in the voltage and current ratings of IGBTs and MOSFET power modules has made it possible to combine both SVC and APF functions in the same Inverter at distribution levels (i.e. at 440V, 1.1kV, 3.3kV, 6.6kV and 11kV levels).

The control of a single-phase APF using hysteresis current control is given in Fig.3. The D.C voltage across the capacitor is sensed, compared with reference and the error is processed in a PI controller. This error multiplies a fixed amplitude sine wave which is pure and in 180° phase with the reference. The product forms one component of the current reference of the Inverter. The harmonic current calculator receives the load current signal from the CT in the load line and a pure sine wave template from the control system and calculates the harmonic current component in the load in real time. The output of this calculator forms the second component of reference current. These two components are added together and given as current reference into a hysteresis current controller.
3. **Current Control Schemes Suitable for APF**

The block diagram above assumed hysteresis current control and hysteresis current control is indeed suitable if only low order harmonics (like 3rd, 5th, 7th etc.) need be compensated. However, if harmonics up to 25th or so are to be cancelled, hysteresis control will require excessively high switching frequency. In addition, the variation in switching frequency which is basic to hysteresis control makes it difficult to choose filter components. Hence constant switching frequency, unipolar switching schemes are preferred for implementing current control of Inverter in APF application as a rule.

In one constant switching frequency current control scheme, the filter inductor current is sensed and compared directly with the reference current to form the current error. This error is amplified and used as the modulating signal in the unipolar pulse width modulator which controls the gating of switches. This scheme suffers from some disadvantages. First, the current sensed will have switching ripple in it and it will have to be filtered before getting into the high gain error amplifier. This filtering introduces a time delay. Already the system is of second order due to the $L_f$ and $C_f$. This second order dynamics has sharp phase angle variation near its resonance frequency due to its underdamped nature. In addition, the phase delay contributed by it depends strongly on the operating condition. Now if a high gain stage with a first order filter is put in the feedback path, the system easily becomes unstable. Even if it is stable, its transient response will not be satisfactory. This will call for reduction of gain in the error amplifier which will affect the ability of the APF to track the reference current adversely. If a high gain has to be used then a high switching frequency becomes mandatory.

Secondly, the current that is being sensed is current in a switching system and will be corrupted by the inevitable high frequency switching noise. The control loop usually gets thoroughly upset with this noisy feedback.

These limitations of feedback control scheme provided the motivation for the development of a feed-forward control scheme for the control of current in the Inverters. The principle of this scheme follows.

Assuming the control is successful, the current that will flow through $L_f$ is known *apriori* and it is equal to the reference current. Then, if the $I_f$ value is known beforehand, the voltage that the Inverter should generate in order to make this current flow can be calculated and the calculation result (a voltage signal) can be given as the modulating signal for the unipolar PWM generator. The voltage that the Inverter should generate is given below by applying K.V.L.

$$V_{inv} = V_{ac} + R I_{ref} + L_f \left(\frac{dI_{ref}}{dt}\right)$$

where $I_{ref}$ is the current commanded by the control system, $R$ is the equivalent loss resistance (includes winding resistance, switch power loss etc.), $L_f$ is the filter inductance and $V_{ac}$ is the source voltage. A simple Opamp circuit can implement the above equation by accepting a stepped down version of source voltage and the reference current signal as the inputs. The output of the circuit is given to...
the unipolar PWM circuit after suitable scaling. Then the Inverter generates the right voltage and hence the current in $L_f$ will have to be $I_{\text{ref}}$.

However, this requires the knowledge of accurate values of $R$ and $L_f$. The value of $R$ is operating point dependent (through switch power losses) and can not be known accurately. If these values are precisely known the current control would have been 'free of dynamics' i.e., the bandwidth of current control loop would have been infinite. But there are inaccuracies in the estimation of the parameters and inaccuracies in the measurement of $V_{ac}$. Also the differentiator operation has to be band limited in practice due to the well known sensitivity of differentiator to noise and high frequency signals. These imperfections make the current control logic deviate from the ideal and a small amount of actual current feedback will be needed along with the other components to correct the minor deviations. However, now the role of current feedback is only to correct second order effects and hence can be of low gain. Moreover, for the same reason no filtering is needed in the feedback path. With this term added, the Inverter voltage control equation becomes:

$$V_{\text{inv}} = V_{ac} + R I_{\text{ref}} + L_f \frac{d(I_{\text{ref}})}{dt} + K (I_{\text{ref}} - I_L)$$

where $K$ is the feedback gain and is usually very small. This scheme is capable of rise time of $50\mu s\text{ to }250\mu s$ and yields a high bandwidth current control loop which is highly desirable in APF since APF is expected to track up to 25th harmonic and more.

$$K$$ is the feedback gain, $K_{\text{pwm}}$ is the gain of Inverter and $Z_0(s)$ is the equivalent load impedance connected at the a.c source point.

4. The D.C Voltage Control Loop

The D.C voltage control loop in APF is similar to the D.C control loop of Active Line Conditioners or PWM Rectifiers, Static VAr Compensators etc, and similar considerations apply.

The instantaneous power input into the inverter (due to harmonic currents, fundamental active current needed to supply the inverter losses and fundamental reactive power if static VAr compensation is also being performed) from mains will get balanced by (i) the dissipation in the inverter and capacitor (ii) the rate of change of stored energy in the inverter passive filter reactive elements and (iii) rate of change of stored energy in the DC Side Capacitor. The inverter losses and the power that goes into changing the energy storage in the small filter elements may be ignored in a first order qualitative analysis and we may say that to a good approximation the instantaneous power that goes into the inverter reaches the DC Side capacitor. Fundamental current flow (which will be a small active component if no shunt VAr compensation is being done) will result in second harmonic pulsations in the inverter input power and this should lead to second harmonic voltage components appearing across DC side capacitor. Harmonic current flow into inverter similarly will give rise to higher harmonic voltage ripples in the DC Side Capacitor. The second harmonic ripple in voltage across the DC Side capacitor can cause some difficulty in the DC voltage control loop. The problem becomes significant if the inverter is doing VAr control as well as harmonic control.

When the DC Side voltage is sensed, compared with a set reference and the error is amplified the second harmonic (and higher harmonics in capacitor voltage) get amplified and appear at the output of the
error amplifier. The second harmonic at the error amplifier output results in a third harmonic component appearing in the reference current and this will lead to injection of third harmonic current in the line. The DC side voltage will have to be filtered to remove the second harmonic to prevent this. This filtering will invariably slow down the DC voltage control loop which in turn will call for a higher value of DC side capacitance.

However, since the 50 Hz current in the Inverter line of an APF is small, the DC side capacitor will not have much second harmonic ripple and hence not much filtering is required on this voltage before it gets into the control loop if the APF will never be required to do static VAr compensation too. By the same reason, the DC loop control can be faster in APF compared to APLC, SVC or Switched Mode Rectifier.

5. **The Harmonic Current Calculator**

This is the most important component in the control system. It accepts the load current and sinusoidal templates from the PLL-Sine wave generator and returns the value of harmonic content of the load current for further control purposes. The D.C side capacitor should not be asked to supply even a fraction of the active power required by the load since it will run down rapidly if that happens. Hence, the Calculator must ensure that neither under steady state nor under load transient conditions the calculated current will contain an active fundamental component. However, it is not possible to ensure this under transient conditions strictly. Then the Calculator must reduce the active component to zero as fast as possible. Any delay on the part of this Calculator in removing the active power component in its output will be translated as higher and higher value for the D.C side capacitor especially considering the unavoidable filtering in the DC voltage control loop.

The method for extracting the reactive fundamental component contained in a sinusoidal current is based on extraction of orthogonal fundamental frequency components from the waveform. The sensed load current is multiplied with unit amplitude sine and cosine waves (produced by PLL + EPROM method). The products are integrated over one half cycle. The value of integrated outputs are sampled and held at the end of the half cycle period and after sampling the integrators are reset briefly to start the next cycle of integration. The sampled outputs will be the amplitude of active and reactive component respectively. The unit sine and cosine templates are multiplied by these amplitudes to re-create the active and reactive fundamental components and their sum is subtracted from the total load current. The result will be the instantaneous harmonic content in the load current and this is sent to the output. Obviously, the maximum delay in the calculation is one half-cycle time. This method of harmonic component calculation is insensitive to the presence of harmonics in supply voltage. If the both the supply voltage and load current contain harmonics it is possible that some active power transfer is taking place through harmonics. Then these active power components will be missed out by this calculator; but then the voltage control loop will handle this. However this method is sensitive to supply frequency and component tolerances and can result in wrong estimates of harmonic components if frequency varies over a wide range. This scheme is illustrated in Fig. 5(a).

![Fig. 5(a) Harmonic Extraction Based on Orthogonality Principle](image)

If the products of load current and unit sine/cosine templates are passed through low pass filters of cutoff around 10Hz (to avoid 100Hz components in the products) we can get the active and reactive
fundamental components of the load current. Subtracting these components from the total will lead us to the harmonic content. And in order to make the circuit rugged against parameter inaccuracies and variations the following closed loop system has been suggested. (See “A Simple Frequency Independent Method for Calculating the Reactive and Harmonic Current in a Nonlinear Load”, J. Sebastian Tepper et.al, IEEE Trans. On Industrial Electronics, Vol 43, No 6, Dec 1996, pp 647-654)

The low pass filter in this scheme has to be of very low bandwidth, otherwise the second harmonic that comes through will manifest as third harmonic in the line current. But then a low bandwidth in the LPF will make the circuit very slow and when a sudden load change takes place all the load current will come through in name of “harmonics” because of delayed response of LPF. This will lead to inverter trying to support the load active power for too long - the result is too heavy a value for the DC Side Capacitor. This scheme is illustrated in Fig. 5(b).

![Diagram](image)

**Fig. 5(b)** Frequency independent Extraction of Harmonics

6. **Simulation Results**

An example shunt APF using a 230V, 50Hz, 500VA Single Phase Full Bridge Inverter using IRFP450 MOSFETs as the power converter was simulated in PSpice with an aim towards providing some realistic sample waveforms to the reader. An inductance of 1mH and a shunt connected capacitance of 2 uF carry out the filtering of inverter output to remove the switching frequency components. The output of the inverter is tied to the a.c supply and a non-linear load is supplied from the point of common coupling. The inverter uses unipolar PWM using triangular carrier of 20kHz. The inverter works in the current regulated mode using feed forward method of current control.
Case 1  Rectifier Load 300W with 330μF Capacitor Filter switched on at t=0 and switched off at t=100ms and line at 230V r.m.s.

Fig.6 shows the simulation waveforms in this case.

The source current is seen to be a good sine wave. The rectifier stops drawing load current at t=100ms. However the effect of this will be felt in the current control loop since the feedback is based on a sampling scheme. The information on how much active power and reactive power were drawn by the load in an
a.c cycle will be available only at the end of that cycle in the harmonic current calculator block. In other words, there is a maximum of one cycle delay between change in load current and change in the harmonic current calculated by the harmonic current calculator. Hence the source current continues to be at the same old level for one more cycle after the 100ms point. But, now since there is no load to absorb this power it will go into inverter and charge up the d.c side capacitor. This is clearly seen in the capacitor voltage waveform. The set value of capacitor voltage is 400V and as the capacitor approaches that level the source current tapers down to zero. Close examination of the source voltage and source current waveforms reveal that there is a sudden phase change of 180 deg in source current at 120ms and that after that time point the power flow is into the source. It is as it should be since the capacitor is overcharged now and the system has to pump energy back into the source in order to bring the capacitor back to its set value.

Fig.7 shows the spectral analysis of the relevant currents when the 300W rectifier was drawing power. The low frequency harmonics in source current are in the 10-50mA range indicating almost pure sine wave current. Note that the inverter current and the rectifier current are harmonic rich.

The simulation model employed makes an assumption that whatever voltage is demanded of the inverter by the current regulation loop can really be synthesised by the inverter. This is not true. The maximum voltage that an inverter can synthesise is equal to the d.c side voltage theoretically. But there are restrictions on minimum and maximum pulse widths that can be realised in an inverter practically. Due to these restrictions the practical inverter can utilise only a maximum of 95% of d.c voltage. These practical limits are ignored in this simulation and it is assumed that the inverter can utilise the d.c side voltage fully. This is why there is a limiter set at ±380V in the inverter model. This assumes that d.c side is maintained at 400V. But during transients d.c voltage varies. Hence after simulation run is over the result should be checked to see that at no time the inverter synthesised voltage was above the capacitor voltage. In case-1 the maximum inverter demand was 360V and the capacitor voltage never went below 382Volts. Hence the simulation results for case-1 will be acceptable.

**Case-2** Full Bridge Thyristor Converter Load 500W with negligible smoothing inductor on d.c side, line at 230V r.m.s.

![Fig.8 Waveforms for Case-2](image)

Fig.8 shows the simulation output. The load waveform has sharp change at the firing instant due to low level of smoothing inductance (the load circuit time constant was 20uS) in the d.c side. Inverter has to absorb this sudden change in current if the supply current is to become pure sine. But if the inverter current changes suddenly the filter inductance will demand a very high voltage. This high voltage can not be supplied by the inverter due to limited value of d.c side voltage. Hence the inverter output goes to the maximum possible and gets clamped there as evident in the form of narrow pulses in the waveform in fig.8. Thus the inductance gets only a limited voltage (the difference between maximum inverter output and peak supply voltage) and hence its current slews up only gradually. This results in the supply line taking the sudden changes in load current which is
clearly visible in the supply current waveform in Fig.8. Thyristor converter fed resistive load is the most demanding load on an Active Power Filter and waveform improvement on supply side will be only partial as illustrated in this case study.

In this case also the capacitor voltage was verified to be above the inverter output at all time and hence simulation results are acceptable.

Case-3 Same as in case – 2 but the load circuit time constant was changed to 200µS.

Fig.9 shows the relevant waveforms in this case. The source current is seen to be almost pure sine wave in this case.

7. Determining Active Filter Ratings for Non-linear Load Types

One of the confusing aspects of applying active filters is trying to figure out the active filter rating that is required to compensate for the harmonics from a particular load. A parallel-connected active filter should be rated in terms of the rms current it can provide. Then the task is to figure out the rms current required to compensate for the harmonics from different types of loads. Simulations will be needed for a number of typical non-linear loads to develop some guidelines for active filter ratings.

One advantage of the parallel-connected active filter, as compared to passive filters, is that it is self-limiting in terms of the harmonic cancellation provided. There is no concern for overloading the filter due to harmonics from the utility supply system or under-rating the filter for the loads involved. The worst case scenario if the filter is under-rated is that it just won’t completely compensate for all the non-linear load current harmonics. In fact, it may not be necessary to compensate for all the harmonics from a non-linear load. With the active filter, the size can be selected to achieve any desired level of cancellation. One good way to use this concept would be to provide only enough compensation so that the load/filter compensation was within some specified guidelines for harmonic generation (e.g. IEEE 519-1992).

8. Effect of Load Waveform on Filtering Effectiveness

The effectiveness of the active filter in compensating for harmonic components of the load current depends on the specific load current waveform involved. Two different waveforms may have the same rms harmonic content but the active filter may do a better job of compensating for one of the waveforms because of the waveshapes involved.
An ac voltage regulator is used for illustration. Two cases are compared in Figure 10. The only difference between the two cases is the load of the ac regulator. In the waveforms on the left side of the figure, the load is a pure resistance. The waveforms on the right side are for the case where the load is a series combination of resistance and reactance. The performance is much better for the smoother load current waveform (RL load). It is worthwhile to note that the majority of applications for the active filter will involve waveforms like those on the right hand side of Figure 10 (e.g. adjustable speed drives with diode bridge rectifiers or single phase electronic loads), rather than the left side.

In general, the current waveform of an ac regulator with resistive load is an example of the waveshape that poses the severest challenge for an active filter. The problem is the high di/dt that is required of the filter to compensate for the high di/dt at turn on of the regulator. The problem is most severe when the regulator is turned on with a firing angle close to 90 degrees because this is when the available driving voltage stored on the dc capacitor is at a minimum. The output di/dt capability can be raised either by increasing the dc voltage setting or by reducing the size of the interfacing inductance. The problem is most severe when the regulator is turned on with a firing angle close to 90 degrees because this is when the available driving voltage stored on the dc capacitor is at a minimum. The output di/dt capability can be raised either by increasing the dc voltage setting or by reducing the size of the interfacing inductance. The limiting factor for increasing the dc voltage is the voltage withstand capability of the IGBT devices. The limiting factors for reducing the interfacing inductance include the IGBT di/dt withstand capability, control requirements, the interface passive filter requirement, and overall system stability. If the interfacing inductance becomes too small, the dc voltage cannot be kept constant for normal operation.

9. Steady-State Rating Requirements

The best way to provide a rating for an active filter is in terms of the rms current that it must provide to compensate for harmonics from non-linear loads. Table 1 provides a convenient summary of different non-linear load types with example waveforms and typical levels of harmonic current distortion associated with each load. Using these typical waveforms, it is possible to calculate a theoretical value for the required harmonic compensation from the active filter. The summary includes the THD for each non-linear load waveform and the required active filter rating in rms amps per kVA of load rating. These ratings assume that the active filter rating should be based on the total rms harmonic current content of the load. A simulation waveform illustrating the active filter effectiveness for each of these waveforms is also provided. The ratings in Figure 11 (next page) assume ideal active filter characteristics. That is, they assume that the active filter can compensate for every amp of harmonic current created by the non-linear load.
<table>
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<tr>
<th>Type of Load</th>
<th>Nonlinear Load Current Waveform</th>
<th>Supply Current with Active Filter</th>
<th>Nonlinear Load Current THD (%)</th>
<th>Active Filter Rating (ms Amps/KVA of Load)</th>
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II. HARMONIC VOLTAGE CANCELLATION & ISOLATION BY SERIES ACTIVE POWER FILTERING (SPAF) IN DISTRIBUTION SYSTEMS

1. Introduction

In Shunt Active Power Filtering, the Inverter injects harmonic currents required for elimination of harmonics in the source current and injects it at the node where the load is connected. The current drawn by the Inverter is forced to contain a small in-phase sinusoidal component in order to draw enough active power from source to supply losses in the APF and to maintain the D.C side capacitor voltage constant. Series APF is the dual of Shunt APF.

In Series APF the Inverter injects a voltage in series with the line which feeds the polluting load through a transformer. The injected voltage will be mostly harmonic with a small amount of sinusoidal component which is in-phase with the current flowing in the line. The small sinusoidal in-phase (with line current) component in the injected voltage results in the right amount of active power flow into the Inverter to compensate for the losses within the Series APF and to maintain the D.C side capacitor voltage constant. Obviously, the D.C voltage control loop will decide the amount of this in-phase component.

Depending upon the location of Series APF, nature of bus voltage and nature of load the purpose of injecting harmonic voltage in series with the line can be one of the following.

(i) In this case the distribution bus (say 11 kV) is polluted and has non-negligible harmonic content. It is required to clean up this voltage before it reaches sensitive loads. Essentially we want to remove the harmonic content in the voltage at the distribution substation before it is fed into a feeder supplying harmonic-sensitive loads. The bus voltage corruption may have been due to harmonic current generating loads upstream. However, the Series APF is not aimed at that harmonic generation problem; but is applied to protect other chosen loads from the already present harmonics in the source bus. In this mode, the Series APF senses the bus voltage and line currents and injects the right amount of harmonic voltages in series with the line in such a way that the voltages after the filter will be harmonic free and clean. Fig.1 shows the power circuit and control blocks of a Series APF working in this mode. This mode of operation can be termed Harmonic Cancellation Mode since the Series APF in this mode cancels the harmonics present in the source voltage before it gets to the load.

![Fig.1 Series Active Filter Power Circuit and Control System](image-url)
In the second context, a Series APF is used to help a shunt connected Passive Filter in diverting the harmonic currents generated by a non-linear load. Tuned LC filters are supposed to have zero impedance at the tuning frequency. However, they will have non-zero value due to losses in the inductor. Hence, the tuned filter shares the harmonic current with the line and source impedance instead of absorbing it entirely. Moreover, the filter is easily detuned with ageing of components and degradation in capacitors. In addition, changes in system frequency make the filter detuned. If the filter is detuned, the harmonic current generated by the non-linear load will flow in the source path partially thereby reducing the filtering effectiveness of the Passive Filter. One way to increase the effectiveness of the Passive Filter and make it absorb all the harmonic current is to insert a high impedance in series with the line (source) before the load. Of course, this high impedance should be there only for harmonic current flow and it should go to a zero value for fundamental current flow.

The Series APF in this mode of operation, senses the harmonic current flow in the line and forces the Inverter to inject (through a transformer) a harmonic voltage proportional to this current in series with the source in direction to oppose the current flow—in short the Series APF simulates a high resistance in series with the line for harmonic currents alone. With this high resistance in the source side, the Passive Filter is forced to absorb all the harmonic current generated by the load even if it has a non-zero impedance at the harmonic frequency due to detuning.

Of course, the load voltage will become distorted if the filter impedance is not zero. Moreover, a single tuned LC filter will take care of only one harmonic component. It needs multiple LC filters to handle all the major harmonics. All the LC sections will derive benefit from the same Series APF. If there are harmonic components which the Passive Filters can not absorb without distorting load bus voltage beyond acceptable levels, they will have to be permitted to flow into the source by Series APF presenting a low or zero resistance those frequency components. The Series APF used in this mode of operation is called \textit{Harmonic Isolator} since it isolates the source bus at high frequencies from the polluting load.

2. The Series APF in Harmonic Cancellation Mode

Fig. 1 shows a Series APF in this mode. The source \( V_{\text{S}} \) and inductance \( L_{\text{S}} \) represent the Thevenin’s equivalent of the power system behind the distribution bus. \( V_{\text{lb}} \) is the source bus voltage which contains harmonics. Line represents the line inductance of the feeder feeding the load bus. \( V_{\text{lb}} \) is the load bus voltage. The Series APF injects \( V_{\text{i}} \) in series with the line as shown. Single-Phase topology is considered in the interest of simplicity.

The line current \( I \) is sensed by a CT and converted to electronic level and is fed into a PLL-Counter-EPROM-DAC type sine wave generator. This block generates unit amplitude pure Sine wave which is in phase with the feeder line current. It also outputs a unit amplitude Cosine wave. The harmonic content of the source bus voltage (and thereby the voltage that the APF must inject into line) can be found out by subtracting the fundamental component of bus voltage from the total bus voltage. This requires the extraction of fundamental component.

The sensed bus voltage is multiplied with unit Sine and Cosine respectively to extract the fundamental orthogonal components of voltage. The products are integrated for a cycle duration and the value of integrals is noted by a sample and hold mechanism at the end of cycle period. After sampling the integrators are reset and allowed to perform the integration for the next period. The sampled values will give the amplitude of in-phase and quadrature (with respect to line current) fundamental components of voltage. These amplitudes are multiplied with appropriate sinusoidal templates and added to re-construct the net fundamental component of voltage and then it subtracted from the total bus voltage to get the harmonic content.

The D.C. side capacitor voltage will discharge down to zero unless sufficient power is drawn from the line to meet the losses in the Inverter. This power is drawn by injecting a fundamental in-phase component against the line current flow. The amount of this component is decided by a PI controller which monitors the D.C. bus voltage.

The Inverter in the Series APF carries the full line current (after transformation). But the voltage generated at the output has only a small fundamental component and has mostly harmonic components (usually 5th, 7th, 11th etc.). Therefore the a.c side power in the inverter will be at 4th, 6th, 8th harmonic etc. Thus, the reactive power flow into the D.C. side capacitor is at those frequencies and the ripple across the capacitor can be made small due to high frequency nature of these power components. Also, the kVA rating of Inverter and D.C side capacitor will be decided by the harmonic content in the voltage and the maximum line current.

The control system design considerations for the D.C. voltage control loop has been described already described in other contexts (SVC, Shunt APF, PWM Rectifier etc.) and need not be repeated here. The
crucial control block in this application is the harmonic content calculator. The calculator has to ensure that the output from it does not contain any in-phase component. If it contains that the capacitor will either discharge fast or overcharge and in order to limit the change in capacitor voltage before the voltage control loop can act ,it will be necessary to use large valued capacitor. The calculator will ensure that there is no fundamental component in its output under steady conditions. But under transient conditions (change in line current, changes in bus voltage etc.), it may output fundamental component. The value of D.C side capacitor will be decided almost entirely by the dynamic response of this Calculator block.

The most difficult thing about a Series APF is to protect it. Note that it is in series with the line and has to carry all the load current (fundamental plus harmonic, if any). Moreover, the fault currents also will pass through it. It is not enough to shut down the Inverter based on fast over current sensing because if the Inverter is shut down the transformer primary goes open and secondary imposes a large impedance in series with the line. A Series APF is to be shorted to take it out of service i.e. it has to be taken out of line and a sort path has to be put in its place. This can call for fast acting static transfer switches.

The Series APF effectively cancels the entire harmonic content of source bus voltage. Now what if the load at the load bus is non-linear ? The harmonic currents drawn by the load via the line will flow through the Thevenin's impedance of the source (L_s) and produce further harmonic voltages at the source bus. But these also will get cancelled by the Series APF i.e. the Series APF makes the harmonic impedance to its left side zero. Hence the harmonic impedance of the line plus source is reduced by Series APF and any shunt filter put at the load bus will have to compete with a lower harmonic impedance in the harmonic current sharing process. In particular , if this Series APF is installed at the load bus i.e. after the line ,a passive shunt filter (like capacitor or tuned LC etc.) is going to be completely useless and all the harmonic current will go into the line, thereby corrupting the voltage received by other loads which are not protected by a Series APF. Of course it is possible to install a Shunt Active Filter at the load bus to cancel the harmonic currents taken by load.

3. The Series APF as a Reactance Compensator

In the last section it was pointed out that the harmonic voltage calculator has the in-phase and out-of-phase sine waves available to it in order to arrive at an estimate of net fundamental component in the voltage. The injected voltage is harmonic plus a little in-phase fundamental component required to draw the loss power. Now, if the injected voltage reference is made to have a sinusoidal component which is in quadrature with line current, the Series APF will absorb or deliver fundamental frequency reactive power. It becomes a series reactive power compensator or equivalently it becomes a reactance at fundamental frequency. Series APF in this mode can provide series capacitor/inductor compensation to the line along with harmonic cancellation. The required voltage reference can be obtained using the Cosine wave template already available in the control system. Of course, the kVA rating of Inverter and other components will have to be suitably chosen.

This series compensation capability can be made use of in two ways. In one case, it can be controlled in such a way that it injects a fundamental voltage in quadrature with the line current in proportion to the current magnitude. In that case, the Series APF becomes a fixed reactance value at fundamental frequency - usually capacitive. The application of series capacitors in the transmission lines to improve power transfer capability, system stability and voltage regulation is well known. Series APF can implement this series capacitor compensation as explained above.

A second way in which the fundamental Var compensation capability of Series APF can be employed is by using it to regulate the voltage after the Series APF location at a pre-decided value. This can be done by sensing the voltage magnitude downstream, comparing it with a set value, processing the error in a PI Controller and using the error to multiply Cos(\(\omega t + 180^\circ\)) . The product is added along with the harmonic reference coming from the Harmonic Content Calculator to form the net reference signal for the PWM Inverter. Thereby the value of effective capacitive reactance at fundamental frequency simulated by the Series APF is varied to maintain a constant amplitude a.c voltage at a point after the Series APF.

In both ways of implementing the Var compensation action, it is possible to derive additional advantage from Series APF in the form of a fault current limiting reactance (provided the Series APF has high overload capability for short duration). When the sensed line current indicates the occurrence of a fault (either by p.f angle or by its magnitude) the Series APF fundamental reference can be shifted from \(-\cos \omega t\) to \(+\cos \omega t\). Then the Series APF will simulate an inductive reactance and thereby limit the fault current. Series APF is used for this function too in practice.
4. The Series APF in Harmonic Isolation Mode

Fig. 2 shows a Series APF in harmonic isolation mode where it serves to isolate the source from the harmonic currents drawn by the load. It does this by simulating a high resistance in series with the line for harmonic current flow. Only one tuned passive filter is shown at the load bus and it is assumed that the load draws only one harmonic component predominantly. Otherwise, more tuned filters are needed at the load bus.

The source current $I_s$ is sensed and a pure sine wave is in phase with it is generated by the PLL subsystem. The sine thus generated is used to extract the harmonic content in the source current using the orthogonal decomposition method which has been described in the last section. The extracted harmonic component of $I_s$ is multiplied by a gain $K$ and that (along with the small fundamental component needed to draw the loss power) is given as the reference to the PWM Voltage Source Inverter. Thus, the Inverter injects a harmonic voltage which is proportional to the harmonic current into the line, thereby simulating a resistance of value $K$ ohms in the line (only for harmonic current flows).

Now, the harmonic current drawn by the load has two parallel paths to choose through the filter and through the line which appears as a high resistance now. It chooses filter path predominantly even if the filter is slightly detuned. Thus, the harmonic current into the source is reduced to very low levels.

Similar action takes place in the case of harmonic content in the source. The high resistance simulated by the Series APF will absorb all the harmonic voltages (for which there are passive filter branches at load end) present in the source bus and isolate the load from supply side harmonics. This is a welcome feature since in the absence of Series APF, the tuned filter would have drawn large currents from source if there were source side harmonics. This would have led to overloading of the filter and would have called for parallel tuned LC section in series with the line to isolate the series tuned filter from supply side harmonics.

With a series tuned LC filter, there is always a chance of system resonances due to parallel resonance between line/source inductance and filter components. The Series APF in the resistance emulation mode will damp these resonances well and will avoid dangerous harmonic amplification.

It is possible to combine series capacitor compensation along with harmonic isolation in this system by suitably modifying the reference signal to the PWM Inverter.
5. **PSpice Simulation of a Series Active Filter in Harmonic Isolator Mode**

*(Also called Hybrid Active Filter)*

The PSpice Simulation diagram (using Design Lab 8.0) for a Single Phase Series APF in Harmonic Isolation mode is given below. The inverter was modelled as an ideal controlled voltage source. A half-controlled thyristor converter is used as load.

![PSpice Simulation Diagram](image)

**Fig. 3** Simplified Schematic for a Series Harmonic Isolator

The simulation run results for a pure sinusoidal source and thyristor load is shown below in Fig. 4. The harmonic calculator takes one half cycle to calculate the harmonic content properly, till then it outputs all the input as the harmonic content; this explains why the inverter had to inject maximum (limited to 50V) in the beginning. This will lead to a large active power outflow from the DC Side of Inverter and will require a suitably sized capacitor to hold the voltage against such outflow (or inflow) of active power. The filter is seen to take a large leading reactive power – expected since passive filtering is practically possible only along with passive capacitor reactive compensation. The value of inductor required for harmonic filtering alone (without fundamental leading reactive power) will be impractically high. The source current, though more or less sinusoidal, shows high frequency content. This is so since the load current has high frequency content, but the passive filter offers low impedance path only for a few harmonics. Thus the current sharing ratio between the Series Inverter equivalent resistance (40 ohms in the simulation) and filter impedance is adversely affected at high frequencies – leading to more of high frequency currents flowing to source side and consequent appearance of high frequency harmonic content at the load terminal voltage.

The simulation results for a distorted source containing 10% fifth harmonic is shown in Fig. 5. Now the source current is distorted perceptibly – since the inverter has to absorb all the source fifth harmonic across it. However, the load voltage is more or less sinusoidal with a little h.f content which is due to the h.f content in load current as explained above. Thus it can be seen that the Series APF handles all those load current harmonics and source voltage harmonics for which there are tuned passive filter structures at load bus well. And it cannot handle the harmonic components for which there is no low impedance path across load bus. The distortion reported in this simulation will be on the optimistic side due to the neglecting of switching frequency filter of the series inverter.
Fig. 4 PSpice Simulation Results for Series APF - Thyristor Load, Pure Sinusoidal Source

Fig. 5 PSpice Simulation Results for Series APF - Distorted Source and Load
It may be better to introduce a high resistance in series with the line using Series Inverter only for those harmonic components for which there is a tuned structure at the load bus. This will require a harmonic calculator that can extract individual harmonics from the line current.

6. **Differences in DC Side Control between Series APFs and Shunt APFs**

   Both Shunt and Series APFs with self-sustained DC bus (i.e., a Capacitor holding DC Voltage constant without any AC-DC Converter to help it to do so) control their DC Side voltage by drawing a small amount of active power from ac side to supply the losses in the inverter. In the Shunt APF this is done by a PI Control loop on the DC Voltage injecting an active current component into the reference current of the APF. Correspondingly a similar control loop will inject a sinusoidal voltage component which is in-phase with the line current to draw/supply the required adjustment power. In the Shunt APF case, the loop gain of this control loop will be directly proportional to the bus voltage magnitude and hence reasonably constant. But in the Series APF case the loop gain of voltage control loop is directly proportional to the fundamental current amplitude in the line i.e the load current and hence is widely variable with line loading level. This is a major problem with the design of this control loop – a loop which is well damped under low load conditions will either be unstable or will be highly oscillatory under full load conditions.

   If the function of Series APF is only harmonic cancellation or isolation (and not load voltage regulation or series reactive compensation) an easy solution to this control problem will be to replace the DC Side with a small rated single phase diode rectifier or a Battery with a Charger. In fact this is how such installations are made in practice. The rating needed of such a converter will be very small and usually is about 3-5% of the line full load capacity. The rating of Series Inverter itself will be about 10-20% of the line capacity depending on the amount of source and load side harmonics and on the extent of detuning and quality of the passive filters.

**Note :-** The Series APF Systems described here can be applied in three phase systems too. Usually Series APFs in three phase systems make use of three single phase inverters feeding a Y-Open Y transformer and in this case the control strategy described here can straightaway be applied on a phase by phase basis. Only that three PLL systems are not needed. A single PLL locked onto first phase along with suitable EPROM storage can generate the six required unit sinusoidal templates. Also, there are a variety of algorithms available for harmonic content extraction which may have standard implementations in DSP hardware. One of those can replace the harmonic extraction procedure described here (but not with much advantage in performance !)